

# Privacy-Preserving Multi-keyword Ranked Search over Encrypted Cloud Data

Ning Cao<sup>†</sup>, Cong Wang<sup>‡</sup>, Ming Li<sup>†</sup>, Kui Ren<sup>‡</sup>, and Wenjing Lou<sup>†</sup>

<sup>†</sup>Department of ECE, Worcester Polytechnic Institute, Email: {ncao, mingli, wjlou}@ece.wpi.edu,

<sup>‡</sup>Department of ECE, Illinois Institute of Technology, Email: {cong, kren}@ece.iit.edu

**Abstract**—With the advent of cloud computing, data owners are motivated to outsource their complex data management systems from local sites to the commercial public cloud for great flexibility and economic savings. But for protecting data privacy, sensitive data has to be encrypted before outsourcing, which obsoletes traditional data utilization based on plaintext keyword search. Thus, enabling an encrypted cloud data search service is of paramount importance. Considering the large number of data users and documents in the cloud, it is necessary to allow multiple keywords in the search request and return documents in the order of their relevance to these keywords. Related works on searchable encryption focus on single keyword search or Boolean keyword search, and rarely sort the search results. In this paper, for the first time, we define and solve the challenging problem of privacy-preserving multi-keyword ranked search over encrypted cloud data (MRSE). We establish a set of strict privacy requirements for such a secure cloud data utilization system. Among various multi-keyword semantics, we choose the efficient similarity measure of “coordinate matching”, i.e., as many matches as possible, to capture the relevance of data documents to the search query. We further use “inner product similarity” to quantitatively evaluate such similarity measure. We first propose a basic idea for the MRSE based on secure inner product computation, and then give two significantly improved MRSE schemes to achieve various stringent privacy requirements in two different threat models. Thorough analysis investigating privacy and efficiency guarantees of proposed schemes is given. Experiments on the real-world dataset further show proposed schemes indeed introduce low overhead on computation and communication.

## I. INTRODUCTION

Cloud computing is the long dreamed vision of computing as a utility, where cloud customers can remotely store their data into the cloud so as to enjoy the on-demand high quality applications and services from a shared pool of configurable computing resources [1]. Its great flexibility and economic savings are motivating both individuals and enterprises to outsource their local complex data management system into the cloud. To protect data privacy and combat unsolicited accesses in the cloud and beyond, sensitive data, e.g., emails, personal health records, photo albums, tax documents, financial transactions, etc., may have to be encrypted by data owners before outsourcing to the commercial public cloud [2]; this, however, obsoletes the traditional data utilization service based on plaintext keyword search. The trivial solution of downloading all the data and decrypting locally is clearly impractical, due to the huge amount of bandwidth cost in cloud scale systems. Moreover, aside from eliminating the local storage management, storing data into the cloud serves no

purpose unless they can be easily searched and utilized. Thus, exploring privacy-preserving and effective search service over encrypted cloud data is of paramount importance. Considering the potentially large number of on-demand data users and huge amount of outsourced data documents in the cloud, this problem is particularly challenging as it is extremely difficult to meet also the requirements of performance, system usability and scalability.

On the one hand, to meet the effective data retrieval need, the large amount of documents demand the cloud server to perform result relevance ranking, instead of returning undifferentiated results. Such ranked search system enables data users to find the most relevant information quickly, rather than burdensomely sorting through every match in the content collection [3]. Ranked search can also elegantly eliminate unnecessary network traffic by sending back only the most relevant data, which is highly desirable in the “pay-as-you-use” cloud paradigm. For privacy protection, such ranking operation, however, should not leak any keyword related information. On the other hand, to improve the search result accuracy as well as to enhance the user searching experience, it is also necessary for such ranking system to support multiple keywords search, as single keyword search often yields far too coarse results. As a common practice indicated by today’s web search engines (e.g., Google search), data users may tend to provide a set of keywords instead of only one as the indicator of their search interest to retrieve the most relevant data. And each keyword in the search request is able to help narrow down the search result further. “Coordinate matching” [4], i.e., as many matches as possible, is an efficient similarity measure among such multi-keyword semantics to refine the result relevance, and has been widely used in the plaintext information retrieval (IR) community. However, how to apply it in the encrypted cloud data search system remains a very challenging task because of inherent security and privacy obstacles, including various strict requirements like the data privacy, the index privacy, the keyword privacy, and many others (see section III-B).

In the literature, searchable encryption [5]–[13] is a helpful technique that treats encrypted data as documents and allows a user to securely search through a single keyword and retrieve documents of interest. However, direct application of these approaches to the secure large scale cloud data utilization system would not be necessarily suitable, as they are developed as crypto primitives and cannot accommodate

such high service-level requirements like system usability, user searching experience, and easy information discovery. Although some recent designs have been proposed to support Boolean keyword search [14]–[21] as an attempt to enrich the search flexibility, they are still not adequate to provide users with acceptable result ranking functionality (see section VI). Our early work [22] has been aware of this problem, and provided a solution to the secure ranked search over encrypted data problem but only for queries consisting of a single keyword. How to design an efficient encrypted data search mechanism that supports multi-keyword semantics without privacy breaches still remains a challenging open problem.

In this paper, for the first time, we define and solve the problem of multi-keyword ranked search over encrypted cloud data (MRSE) while preserving strict system-wise privacy in the cloud computing paradigm. Among various multi-keyword semantics, we choose the efficient similarity measure of “coordinate matching”, i.e., as many matches as possible, to capture the relevance of data documents to the search query. Specifically, we use “inner product similarity” [4], i.e., the number of query keywords appearing in a document, to quantitatively evaluate such similarity measure of that document to the search query. During the index construction, each document is associated with a binary vector as a subindex where each bit represents whether corresponding keyword is contained in the document. The search query is also described as a binary vector where each bit means whether corresponding keyword appears in this search request, so the similarity could be exactly measured by the inner product of the query vector with the data vector. However, directly outsourcing the data vector or the query vector will violate the index privacy or the search privacy. To meet the challenge of supporting such multi-keyword semantic without privacy breaches, we propose a basic idea for the MRSE using secure inner product computation, which is adapted from a secure  $k$ -nearest neighbor ( $kNN$ ) technique [4], and then give two significantly improved MRSE schemes in a step-by-step manner to achieve various stringent privacy requirements in two threat models with increased attack capabilities. Our contributions are summarized as follows,

- 1) For the first time, we explore the problem of multi-keyword ranked search over encrypted cloud data, and establish a set of strict privacy requirements for such a secure cloud data utilization system.
- 2) We propose two MRSE schemes based on the similarity measure of “coordinate matching” while meeting different privacy requirements in two different threat models.
- 3) Thorough analysis investigating privacy and efficiency guarantees of the proposed schemes is given, and experiments on the real-world dataset further show the proposed schemes indeed introduce low overhead on computation and communication.

The remainder of this paper is organized as follows. In Section II, we introduce the system model, the threat model, our design goals, and the preliminary. Section III describes

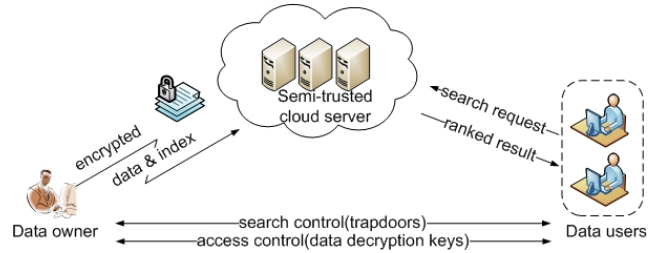


Fig. 1: Architecture of the search over encrypted cloud data

the MRSE framework and privacy requirements, followed by section IV, which describes the proposed schemes. Section V presents simulation results. We discuss related work on both single and Boolean keyword searchable encryption in Section VI, and conclude the paper in Section VII.

## II. PROBLEM FORMULATION

### A. System Model

Considering a cloud data hosting service involving three different entities, as illustrated in Fig. 1: the data owner, the data user, and the cloud server. The data owner has a collection of data documents  $\mathcal{F}$  to be outsourced to the cloud server in the encrypted form  $\mathcal{C}$ . To enable the searching capability over  $\mathcal{C}$  for effective data utilization, the data owner, before outsourcing, will first build an encrypted searchable index  $\mathcal{I}$  from  $\mathcal{F}$ , and then outsource both the index  $\mathcal{I}$  and the encrypted document collection  $\mathcal{C}$  to the cloud server. To search the document collection for  $t$  given keywords, an authorized user acquires a corresponding trapdoor  $T$  through search control mechanisms, e.g., broadcast encryption [8]. Upon receiving  $T$  from a data user, the cloud server is responsible to search the index  $\mathcal{I}$  and return the corresponding set of encrypted documents. To improve the document retrieval accuracy, the search result should be ranked by the cloud server according to some ranking criteria (e.g., coordinate matching, as will be introduced shortly). Moreover, to reduce the communication cost, the data user may send an optional number  $k$  along with the trapdoor  $T$  so that the cloud server only sends back top- $k$  documents that are most relevant to the search query. Finally, the access control mechanism [23] is employed to manage decryption capabilities given to users.

### B. Threat Model

The cloud server is considered as “honest-but-curious” in our model, which is consistent with related works on cloud security [23], [24]. Specifically, the cloud server acts in an “honest” fashion and correctly follows the designated protocol specification. However, it is “curious” to infer and analyze data (including index) in its storage and message flows received during the protocol so as to learn additional information. Based on what information the cloud server knows, we consider two threat models with different attack capabilities as follows.

**Known Ciphertext Model** In this model, the cloud server is supposed to only know encrypted dataset  $\mathcal{C}$  and searchable index  $\mathcal{I}$ , both of which are outsourced from the data owner.

**Known Background Model** In this stronger model, the cloud server is supposed to possess more knowledge than what can be accessed in the known ciphertext model. Such information may include the correlation relationship of given search requests (trapdoors), as well as the dataset related statistical information. As an instance of possible attacks in this case, the cloud server could use the known trapdoor information combined with document/keyword frequency [25] to deduce/identify certain keywords in the query.

### C. Design Goals

To enable ranked search for effective utilization of outsourced cloud data under the aforementioned model, our system design should simultaneously achieve security and performance guarantees as follows.

- **Multi-keyword Ranked Search:** To design search schemes which allow multi-keyword query and provide result similarity ranking for effective data retrieval, instead of returning undifferentiated results.
- **Privacy-Preserving:** To prevent the cloud server from learning additional information from the dataset and the index, and to meet privacy requirements specified in section III-B.
- **Efficiency:** Above goals on functionality and privacy should be achieved with low communication and computation overhead.

### D. Notations

- $\mathcal{F}$  – the plaintext document collection, denoted as a set of  $m$  data documents  $\mathcal{F} = (F_1, F_2, \dots, F_m)$ .
- $\mathcal{C}$  – the encrypted document collection stored in the cloud server, denoted as  $\mathcal{C} = (C_1, C_2, \dots, C_m)$ .
- $\mathcal{W}$  – the dictionary, i.e., the keyword set consisting of  $n$  keyword, denoted as  $\mathcal{W} = (W_1, W_2, \dots, W_n)$ .
- $\mathcal{I}$  – the searchable index associated with  $\mathcal{C}$ , denoted as  $(I_1, I_2, \dots, I_m)$  where each subindex  $I_i$  is built for  $F_i$ .
- $\mathcal{W}$  – the subset of  $\mathcal{W}$ , representing the keywords in a search request, denoted as  $\mathcal{W} = (W_{j_1}, W_{j_2}, \dots, W_{j_t})$ .
- $T_{\mathcal{W}}$  – the trapdoor for the search request  $\mathcal{W}$ .
- $\mathcal{F}_{\mathcal{W}}$  – the ranked id list of all documents according to their relevance to  $\mathcal{W}$ .

### E. Preliminary on Coordinate Matching

As a hybrid of conjunctive search and disjunctive search, “coordinate matching” [4] is an intermediate similarity measure which uses the number of query keywords appearing in the document to quantify the relevance of that document to the query. When users know the exact subset of the dataset to be retrieved, Boolean queries perform well with the precise search requirement specified by the user. In cloud computing, however, this is not the practical case, given the huge amount of outsourced data. Therefore, it is more flexible for users to

specify a list of keywords indicating their interest and retrieve the most relevant documents with a rank order.

## III. FRAMEWORK AND PRIVACY REQUIREMENTS FOR MRSE

In this section, we define the framework of multi-keyword ranked search over encrypted cloud data (MRSE) and establish various strict system-wise privacy requirements for such a secure cloud data utilization system.

### A. MRSE Framework

For easy presentation, operations on the data documents are not shown in the framework since the data owner could easily employ the traditional symmetric key cryptography to encrypt and then outsource data. With focus on the index and query, the MRSE system consists of four algorithms as follows.

- **Setup**( $1^\ell$ ) Taking a security parameter  $\ell$  as input, the data owner outputs a symmetric key as  $SK$ .
- **BuildIndex**( $\mathcal{F}, SK$ ) Based on the dataset  $\mathcal{F}$ , the data owner builds a searchable index  $\mathcal{I}$  which is encrypted by the symmetric key  $SK$  and then outsourced to the cloud server. After the index construction, the document collection can be independently encrypted and outsourced.
- **Trapdoor**( $\mathcal{W}$ ) With  $t$  keywords of interest in  $\mathcal{W}$  as input, this algorithm generates a corresponding trapdoor  $T_{\mathcal{W}}$ .
- **Query**( $T_{\mathcal{W}}, k, \mathcal{I}$ ) When the cloud server receives a query request as  $(T_{\mathcal{W}}, k)$ , it performs the ranked search on the index  $\mathcal{I}$  with the help of trapdoor  $T_{\mathcal{W}}$ , and finally returns  $\mathcal{F}_{\mathcal{W}}$ , the ranked id list of top- $k$  documents sorted by their similarity with  $\mathcal{W}$ .

Both search control and access control are not within the scope of this paper. While the former is to regulate how authorized users acquire trapdoors, the later is to manage users’ access to outsourced documents.

### B. Privacy Requirements for MRSE

The representative privacy guarantee in the related literature, such as searchable encryption, is that the server should learn nothing but search results. With this general privacy description, we explore and establish a set of strict privacy requirements specifically for the MRSE framework.

As for the *data privacy*, the data owner can resort to the traditional symmetric key cryptography to encrypt the data before outsourcing, and successfully prevent the cloud server from prying into the outsourced data. With respect to the *index privacy*, if the cloud server deduces any association between keywords and encrypted documents from index, it may learn the major subject of a document, even the content of a short document [25]. Therefore, the searchable index should be constructed to prevent the cloud server from performing such kind of association attack. While data and index privacy guarantees are demanded by default in the related literature, various *search privacy* requirements involved in the query procedure are more complex and difficult to tackle as follows.

**Keyword Privacy** As users usually prefer to keep their search from being exposed to others like the cloud server, the most important concern is to hide what they are searching, i.e., the keywords indicated by the corresponding trapdoor. Although the trapdoor can be generated in a cryptographic way to protect the query keywords, the cloud server could do some statistical analysis over the search result to make an estimate. As a kind of statistical information, *document frequency* (i.e., the number of documents containing the keyword) is sufficient to identify the keyword with high probability [26]. When the cloud server knows some background information of the dataset, this keyword specific information may be utilized to reverse-engineer the keyword.

**Trapdoor Unlinkability** The trapdoor generation function should be a randomized one instead of being deterministic. In particular, the cloud server should not be able to deduce the relationship of any given trapdoors, e.g., to determine whether the two trapdoors are formed by the same search request. Otherwise, the deterministic trapdoor generation would give the cloud server advantage to accumulate frequencies of different search requests regarding different keyword(s), which may further violate the aforementioned keyword privacy requirement. So the fundamental protection for trapdoor unlinkability is to introduce sufficient nondeterminacy into the trapdoor generation procedure.

**Access Pattern** Within the ranked search, the access pattern is the sequence of search results where every search result is a set of documents with rank order. Specifically, the search result for the query keyword set  $\widetilde{W}$  is denoted as  $\mathcal{F}_{\widetilde{W}}$ , consisting of the id list of all documents ranked by their relevance to  $\widetilde{W}$ . Then the access pattern is denoted as  $(\mathcal{F}_{\widetilde{W}_1}, \mathcal{F}_{\widetilde{W}_2}, \dots)$  which are the results of sequential searches. Although a few searchable encryption works, e.g., [17] has been proposed to utilize private information retrieval (PIR) technique [27], to hide the access pattern, our proposed schemes are not designed to protect the access pattern for the efficiency concerns. This is because any PIR based technique must “touch” the whole dataset outsourced on the server which is inefficient in the large scale cloud system.

#### IV. PRIVACY-PRESERVING AND EFFICIENT MRSE

To efficiently achieve multi-keyword ranked search, we propose to employ “inner product similarity” [4] to quantitatively evaluate the efficient similarity measure “coordinate matching”. Specifically,  $D_i$  is a binary data vector for document  $F_i$  where each bit  $D_i[j] \in \{0, 1\}$  represents the existence of the corresponding keyword  $W_j$  in that document, and  $Q$  is a binary query vector indicating the keywords of interest where each bit  $Q[j] \in \{0, 1\}$  represents the existence of the corresponding keyword  $W_j$  in the query  $\widetilde{W}$ . The similarity score of document  $F_i$  to query  $\widetilde{W}$  is therefore expressed as the inner product of their binary column vectors, i.e.,  $D_i \cdot Q$ . For the purpose of ranking, the cloud server must be given the capability to compare the similarity of different documents to the query. But, to preserve strict system-wise privacy, data

vector  $D_i$ , query vector  $Q$  and their inner product  $D_i \cdot Q$  should not be exposed to the cloud server. In this section, we first propose a basic idea for the MRSE using secure inner product computation, which is adapted from a secure  $k$ -nearest neighbor (kNN) technique, and then show how to significantly improve it to be privacy-preserving against different threat models in the MRSE framework in a step-by-step manner.

##### A. MRSE\_I: Privacy-Preserving Scheme in Known Ciphertext Model

1) *Secure kNN Computation*: In the secure  $k$ -nearest neighbor (kNN) scheme [28], Euclidean distance between a database record  $p_i$  and a query vector  $q$  is used to select  $k$  nearest database records. The secret key is composed of one  $(d+1)$ -bit vector as  $S$  and two  $(d+1) \times (d+1)$  invertible matrices as  $\{M_1, M_2\}$ , where  $d$  is the number of fields for each record  $p_i$ . First, every data vector  $p_i$  and query vector  $q$  are extended to  $(d+1)$ -dimension vectors as  $\vec{p}_i$  and  $\vec{q}$ , where the  $(d+1)$ -th dimension is set to  $-0.5\|p_i\|^2$  and 1, respectively. Besides, the query vector  $\vec{q}$  is scaled by a random number  $r > 0$  as  $(r\vec{q}, r)$ . Then,  $\vec{p}_i$  is split into two random vectors as  $\{\vec{p}_i', \vec{p}_i''\}$ , and  $\vec{q}$  is also split into two random vectors as  $\{\vec{q}', \vec{q}''\}$ . Note here that vector  $S$  functions as a splitting indicator. Namely, if the  $j$ -th bit of  $S$  is 0,  $\vec{p}_i'[j]$  and  $\vec{p}_i''[j]$  are set as the same as  $\vec{p}_i[j]$ , while  $\vec{q}'[j]$  and  $\vec{q}''[j]$  are set to two random numbers so that their sum is equal to  $\vec{q}[j]$ ; if the  $j$ -th bit of  $S$  is 1, the splitting process is similar except that  $\vec{p}_i$  and  $\vec{q}$  are switched. The split data vector pair  $\{\vec{p}_i', \vec{p}_i''\}$  is encrypted as  $\{M_1^T \vec{p}_i', M_2^T \vec{p}_i''\}$ , and the split query vector pair  $\{\vec{q}', \vec{q}''\}$  is encrypted as  $\{M_1^{-1} \vec{q}', M_2^{-1} \vec{q}''\}$ . In the query step, the product of data vector pair and query vector pair, i.e.,  $-0.5r(\|p_i\|^2 - 2p_i \cdot q)$ , is serving as the indicator of Euclidean distance ( $\|p_i\|^2 - 2p_i \cdot q + \|q\|^2$ ) to select  $k$  nearest neighbors. Without prior knowledge of secret key, neither data vector nor query vector, after such a series of processes, can be recovered by analyzing their corresponding ciphertext.

As the MRSE is using the inner product similarity instead of the Euclidean distance, we need to do some modifications on the data structure to fit the MRSE framework. One way to do that is by eliminating the dimension extension, the final result changes to be the inner product as  $rp_i \cdot q$ . However, this scheme is not good enough for our MRSE design. The major reason is that the only randomness involved is the scale factor  $r$  in the trapdoor generation, which does not provide sufficient nondeterminacy in the overall scheme as required by the trapdoor unlinkability requirement as well as the keyword privacy requirement. To provide a more advanced design for the MRSE, we now provide our MRSE\_I scheme as follows.

2) *MRSE\_I Scheme*: In our more advanced design, instead of simply removing the extended dimension in the query vector as we plan to do at the first glance, we preserve this dimension extending operation but assign a new random number  $t$  to the extended dimension in each query vector. Such a newly added randomness is expected to increase the difficulty for the cloud server to learn the relationship among the received trapdoors. In addition, as mentioned in the keyword privacy requirement,

randomness should also be carefully calibrated in the search result to obfuscate the document frequency and diminish the chances for re-identification of keywords. Introducing some randomness in the final similarity score is an effective way towards what we expect here. More specifically, unlike the randomness involved in the query vector, we insert a dummy keyword into each data vector and assign a random value to it. Each individual vector  $D_i$  is extended to  $(n+2)$ -dimension instead of  $(n+1)$ , where a random variable  $\varepsilon_i$  representing the dummy keyword is stored in the extended dimension. The whole scheme to achieve ranked search with multiple keywords over encrypted data is as follows.

- **Setup** The data owner randomly generates a  $(n+2)$ -bit vector as  $S$  and two  $(n+2) \times (n+2)$  invertible matrices  $\{M_1, M_2\}$ . The secret key  $SK$  is in the form of a 3-tuple as  $\{S, M_1, M_2\}$ .
- **BuildIndex** $(\mathcal{F}, SK)$  The data owner generates a binary data vector  $D_i$  for every document  $F_i$ , where each binary bit  $D_i[j]$  represents whether the corresponding keyword  $W_j$  appears in the document  $F_i$ . Subsequently, every plaintext subindex  $\vec{D}_i$  is generated by applying dimension extending and splitting procedures on  $D_i$ . These procedures are similar with those in the secure kNN computation except that the  $(n+1)$ -th entry in  $\vec{D}_i$  is set to a random number  $\varepsilon_i$ , and the  $(n+2)$ -th entry in  $\vec{D}_i$  is set to 1 during the dimension extending.  $\vec{D}_i$  is therefore equal to  $(D_i, \varepsilon_i, 1)$ . Finally, the subindex  $I_i = \{M_1^T \vec{D}_i', M_2^T \vec{D}_i''\}$  is built for every encrypted document  $C_i$ .
- **Trapdoor** $(\mathcal{W})$  With  $t$  keywords of interest in  $\tilde{\mathcal{W}}$  as input, one binary vector  $Q$  is generated where each bit  $Q[j]$  indicates whether  $W_j \in \tilde{\mathcal{W}}$  is true or false.  $Q$  is first extended to  $n+1$ -dimension which is set to 1, and then scaled by a random number  $r \neq 0$ , and finally extended to a  $(n+2)$ -dimension vector as  $\vec{Q}$  where the last dimension is set to another random number  $t$ .  $\vec{Q}$  is therefore equal to  $(rQ, r, t)$ . After applying the same splitting and encrypting processes as above, the trapdoor  $T_{\tilde{\mathcal{W}}}$  is generated as  $\{M_1^{-1} \vec{Q}', M_2^{-1} \vec{Q}''\}$ .
- **Query** $(T_{\tilde{\mathcal{W}}}, k, \mathcal{I})$  With the trapdoor  $T_{\tilde{\mathcal{W}}}$ , the cloud server computes the similarity scores of each document  $F_i$  as in equation 1. WLOG, we assume  $r > 0$ . After sorting all scores, the cloud server returns the top- $k$  ranked id list  $\mathcal{F}_{\tilde{\mathcal{W}}}$ .

With  $t$  brought into the query vector and  $\varepsilon_i$  brought into each data vector, the final similarity scores would be:

$$\begin{aligned}
I_i \cdot T_{\tilde{\mathcal{W}}} &= \{M_1^T \vec{D}_i', M_2^T \vec{D}_i''\} \cdot \{M_1^{-1} \vec{Q}', M_2^{-1} \vec{Q}''\} \\
&= \vec{D}_i' \cdot \vec{q}' + \vec{D}_i'' \cdot \vec{q}'' \\
&= \vec{D}_i \cdot \vec{Q} \\
&= (D_i, \varepsilon_i, 1) \cdot (rQ, r, t) \\
&= r(D_i \cdot Q + \varepsilon_i) + t.
\end{aligned} \tag{1}$$

Note that in the original case, the final score is simply  $rD_i \cdot q$ , which preserves the scale relationship for two queries on

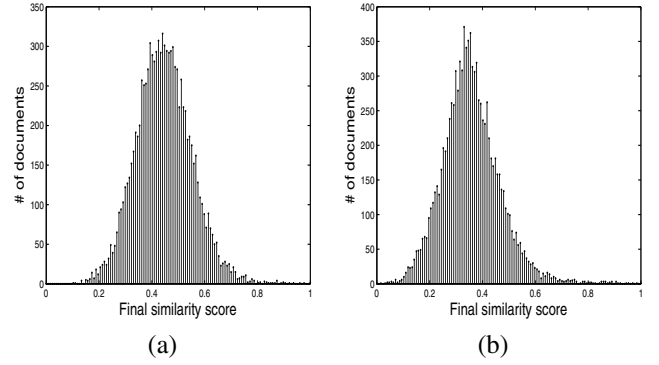


Fig. 2: Distribution of final similarity score with different standard deviations, 10k documents, 10 query keywords. (a)  $\sigma = 1$ . (b)  $\sigma = 0.5$ .

the same keywords. But such an issue is no longer valid in our improved scheme due to the randomness of both  $t$  and  $\varepsilon_i$ , which clearly demonstrates the effectiveness and improved security strength of our MSRE\_I mechanism.

3) **Analysis:** We analyze this MRSE\_I scheme from three aspects of design goals described in section II.

**Functionality and Efficiency** Assume the number of query keywords appearing in a document  $F_i$  is  $x_i = D_i \cdot Q$ . From equation 1, the final similarity score as  $y_i = I_i \cdot T_{\tilde{\mathcal{W}}} = r(x_i + \varepsilon_i) + t$  is a linear function of  $x_i$ , where the coefficient  $r$  is set as a positive random number. However, because the random factor  $\varepsilon_i$  is introduced as a part of the similarity score, the final search result on the basis of sorting similarity scores may not be as accurate as that in original scheme. For the consideration of search accuracy, we can let  $\varepsilon_i$  follow a normal distribution  $N(\mu, \sigma^2)$ , where the standard deviation  $\sigma$  functions as a flexible trade-off parameter among search accuracy and security. From the consideration of effectiveness,  $\sigma$  is expected to be smaller so as to obtain high precision indicating the good purity of retrieved documents. To quantitatively evaluate the search accuracy, we set a measure as precision  $P_k$  to capture the fraction of returned top- $k$  documents that are included in the real top- $k$  list. Detailed accuracy evaluation on the real-world dataset will be given in section VI.

As for the efficiency, our inner product based MRSE scheme is an outstanding approach from the performance perspective. In the steps like **BuildIndex** or **Trapdoor**, the generation procedure of each subindex or trapdoor involves two multiplications of a  $(n+2) \times (n+2)$  matrix and a  $(n+2)$ -dimension vector. In the **Query**, the final similarity score is computed through two multiplications of two  $(n+2)$ -dimension vectors.

**Privacy** As for the *data privacy*, traditional symmetric key encryption techniques could be properly utilized here and is not within the scope of this paper. The *index privacy* is well protected if the secret key  $SK$  is kept confidential since such vector encryption method has been proved to be secure in the known ciphertext model [28]. With the randomness introduced by the splitting process and the random numbers  $r$ , and  $t$ , our

TABLE I:  $K_3$  appears in every document

Doc	Query for $\{K_1, K_2, K_3\}$	Query for $\{K_1, K_2\}$
1	$x_1 = 3, y_1 = r(3 + \varepsilon_1) + t$	$x'_1 = 2, y'_1 = r'(2 + \varepsilon_1) + t'$
2	$x_2 = 2, y_2 = r(2 + \varepsilon_2) + t$	$x'_2 = 1, y'_2 = r'(1 + \varepsilon_1) + t'$
3	$x_3 = 1, y_3 = r(1 + \varepsilon_3) + t$	$x'_3 = 0, y'_3 = r'(0 + \varepsilon_3) + t'$

basic scheme can generate two totally different trapdoors for the same query  $\mathcal{W}$ . This nondeterministic trapdoor generation can guarantee the *trapdoor unlinkability* which is an unsolved privacy leakage problem in related symmetric key based searchable encryption schemes because of the deterministic property of trapdoor generation [8]. Moreover, with properly selected parameter  $\sigma$  for the random factor  $\varepsilon_i$ , even the final score results can be obfuscated very well, preventing the cloud server from learning the relationships of given trapdoors and the corresponding keywords. Note that although  $\sigma$  is expected to be small from the effectiveness point of view, the small one will introduce small obfuscation into the the final similarity scores, which may weaken the protection of keyword privacy and trapdoor unlinkability. As shown in Fig. 2, the distribution of the final similarity scores with smaller  $\sigma$  will enable the cloud server to learn more statistical information about the original similarity scores, and therefore  $\sigma$  should be set large enough from the consideration of privacy.

### B. MRSE\_II: Privacy-Preserving Scheme in Known Background Model

When the cloud server has knowledge of some background information on the outsourced dataset, e.g., the correlation relationship of two given trapdoors, certain keyword privacy may not be guaranteed anymore by the MRSE\_I scheme. This is possible in the known background model because the cloud server can use scale analysis as follows to deduce the keyword specific information, e.g., document frequency, which can be further combined with background information to identify the keyword in a query at high probability. After presenting how the cloud server uses scale analysis attack to break the keyword privacy, we propose a more advanced MRSE scheme to be privacy-preserving in the known background model.

1) *Scale Analysis Attack*: Given two correlated trapdoors  $T_1$  and  $T_2$  for query keywords  $\{K_1, K_2\}$  and  $\{K_1, K_2, K_3\}$  respectively, there will be two special cases when searching on any three documents as listed in Tab. I and Tab. II. In any of these two cases, there exists a system of equations among final similarity scores  $y_i$  for  $T_1$  and  $y'_i$  for  $T_2$  as follows,

$$\begin{cases} y_1 - y_2 = r(1 + \varepsilon_1 - \varepsilon_2); \\ y'_1 - y'_2 = r'(1 + \varepsilon_1 - \varepsilon_2); \\ y_2 - y_3 = r(1 + \varepsilon_2 - \varepsilon_3); \\ y'_2 - y'_3 = r'(1 + \varepsilon_2 - \varepsilon_3). \end{cases} \quad (2)$$

To this end, although the exact value of  $x_i$  is encrypted as  $y_i$ , the cloud server could deduce that whether all the three documents contain  $K_3$  or none of them contain  $K_3$  through checking the following equivalence relationship among all

TABLE II:  $K_3$  does not appear in either document

Doc	Query for $\{K_1, K_2, K_3\}$	Query for $\{K_1, K_2\}$
1	$x_1 = 2, y_1 = r(2 + \varepsilon_1) + t$	$x'_1 = 2, y'_1 = r'(2 + \varepsilon_1) + t'$
2	$x_2 = 1, y_2 = r(1 + \varepsilon_2) + t$	$x'_2 = 1, y'_2 = r'(1 + \varepsilon_1) + t'$
3	$x_3 = 0, y_3 = r(0 + \varepsilon_3) + t$	$x'_3 = 0, y'_3 = r'(0 + \varepsilon_3) + t'$

final similarity scores in two queries,

$$\frac{y_1 - y_2}{y'_1 - y'_2} = \frac{y_2 - y_3}{y'_2 - y'_3} = \frac{y_3 - y_1}{y'_3 - y'_1}. \quad (3)$$

By extending three documents to the whole dataset, the cloud server could further deduce two possible values of document frequency of keyword  $K_3$ . In the known background model, the server can identify the keyword  $K_3$  by referring to the keyword specific document frequency information about the dataset.

2) *MRSE\_II Scheme*: The privacy leakage shown above is caused by the fixed value of random variable  $\varepsilon_i$  in data vector  $D_i$ . To eliminate such fixed property in any specific document, more dummy keywords instead of only one should be inserted into every data vector  $D_i$ . All the vectors are extended to  $(n + U + 1)$ -dimension instead of  $(n + 2)$ , where  $U$  is the number of dummy keywords inserted. Improved details in the MRSE\_II scheme is presented as follows.

- **Setup**( $1^n$ ) The data owner randomly generates a  $(n + U + 1)$ -bit vector as  $S$  and two  $(n + U + 1) \times (n + U + 1)$  invertible matrices  $\{M_1, M_2\}$ .
- **BuildIndex**( $\mathcal{F}, SK$ ) The  $(n + j + 1)$ -th entry in  $\vec{D}_i$  where  $j \in [1, U]$  is set to a random number  $\varepsilon^{(j)}$  during the dimension extending.
- **Trapdoor**( $\mathcal{W}$ ) By randomly selecting  $V$  out of  $U$  dummy keywords, the corresponding entries in  $Q$  are set to 1.
- **Query**( $T_{\mathcal{W}}, k, \mathcal{I}$ ) The final similarity score computed by cloud server is equal to  $r(x_i + \sum \varepsilon_i^{(v)}) + t_i$  where the  $v$ -th dummy keyword is included in the  $V$  selected ones.

3) *Analysis*: Assume the probability of two  $\sum \varepsilon_i^{(v)}$  having the same value should be less than  $1/2^\omega$ , it then means there should be at least  $2^\omega$  different values of  $\sum \varepsilon_i^{(v)}$  for each data vector. The number of different  $\sum \varepsilon_i^{(v)}$  is not larger than  $\binom{U}{V}$ , which is maximized when  $\frac{U}{V} = 2$ . Besides, considering  $\binom{U}{V} \geq (\frac{U}{V})^V = 2^V$ , it is greater than  $2^\omega$  when  $U = 2\omega$  and  $V = \omega$ . So every data vector should include at least  $2\omega$  dummy entries, and every query vector will randomly select half dummy entries. Here  $\omega$  can be considered as a system parameter for the tradeoff between efficiency and privacy. With properly setting the value of  $\omega$ , the MRSE\_II scheme is secure against scale analysis attack, and provides various expected privacy guarantees within the known ciphertext model or the known background model.

Moreover, every  $\varepsilon^{(j)}$  is assumed to follow the same uniform distribution  $M(\mu' - c, \mu' + c)$ , where the mean is  $\mu'$  and the variance as  $\sigma'^2$  is  $c^2/3$ . According to the central limit theorem, the sum of  $\omega$  independent random variables  $\varepsilon^{(j)}$  follows the Normal distribution, where the mean is  $\omega\mu'$  and the variance is  $\omega\sigma'^2 = \omega c^2/3$ . To make  $\sum \varepsilon_i^{(v)}$  follow the Normal distribution

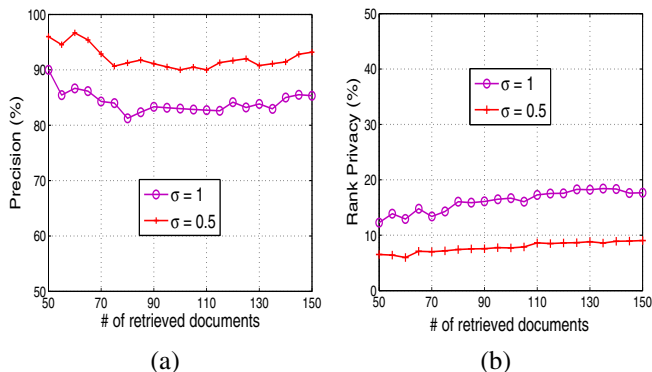


Fig. 3: With different choice of standard deviation  $\sigma$  for the random variable  $\varepsilon$ , there exists tradeoff between (a) Precision, and (b) Rank Privacy.

$N(\mu, \sigma^2)$  as above, the value of  $\mu'$  is set as  $\mu/\omega$  and the value of  $c$  is set as  $\sqrt{\frac{3}{\omega}}\sigma$  so that  $\omega\mu' = \mu$  and  $\omega\sigma'^2 = \sigma^2$ . With such parameter setting, search accuracy is statistically the same as that in MRSE\_I scheme.

## V. PERFORMANCE ANALYSIS

In this section, we demonstrate a thorough experimental evaluation of the proposed technique on a real-world dataset: the Enron Email Dataset [29]. We randomly select different number of emails to build dataset. The whole experiment system is implemented by C language on a Linux Server with Intel Xeon Processor 2.93GHz. The public utility routines by Numerical Recipes are employed to compute the inverse of matrix. The performance of our technique is evaluated regarding the efficiency of two proposed MRSE schemes, as well as the tradeoff between search precision and privacy.

### A. Precision and Privacy

As presented in Section IV, dummy keywords are inserted into each data vector and some of them are selected in every query. Therefore, similarity scores of documents will be not exactly accurate. In other words, when the cloud server returns top- $k$  documents based on similarity scores of data vectors to query vector, some of real top- $k$  relevant documents for the query may be excluded. This is because either their original similarity scores are decreased or the similarity scores of some documents out of the real top- $k$  are increased, both of which are due to the impact of dummy keywords inserted into data vectors. To evaluate the purity of the  $k$  documents retrieved by user, we define a measure as precision  $P_k = k'/k$  where  $k'$  is number of real top- $k$  documents that are returned by the cloud server. Fig. 3(a) shows that the precision in MRSE scheme is evidently affected by the standard deviation  $\sigma$  of the random variable  $\varepsilon$ . From the consideration of effectiveness, standard deviation  $\sigma$  is expected to be smaller so as to obtain high precision indicating the good purity of retrieved documents.

However, user's rank privacy may have been partially leaked to the cloud server as a consequence of small  $\sigma$ . As described

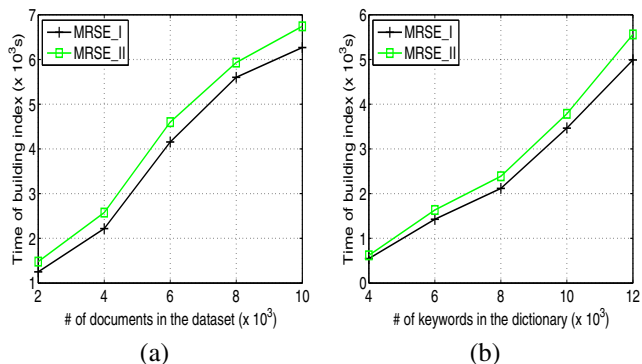


Fig. 4: Time cost of building index. (a) For the different size of dataset with the same dictionary,  $n = 4000$ . (b) For the same dataset with different size of dictionary,  $m = 1000$ .

in section III-B, the access pattern is defined as the sequence of ranked search results. Although search results cannot be protected (excluding costly PIR technique), we can still hide the rank order of retrieved documents as much as possible. In order to evaluate this privacy guarantee, we first define the rank perturbation as  $\tilde{p}_i = |r_i - r'_i|$ , where  $r_i$  is the rank number of document  $i$  in the retrieved top- $k$  documents and  $r'_i$  is its rank number in the real top- $i$  ranked documents. The overall rank privacy measure at point  $k$  is then defined as the average of all the  $\tilde{p}_i$  for every document  $i$  in the retrieved top- $k$  documents, denoted as  $\tilde{P}_k = \sum \tilde{p}_i / k$ . Fig. 3(b) shows the rank privacy at different points with two standard deviations  $\sigma = 1$  and  $\sigma = 0.5$  respectively.

From these two figures, we can see that small  $\sigma$  leads to higher precision of search result but lower rank privacy guarantee, while large  $\sigma$  results in higher rank privacy guarantee but lower precision. In other words, our scheme provides a balance parameter for data users to satisfy their different requirements on precision and rank privacy.

### B. Efficiency

1) *Index Construction*: To build a searchable subindex  $I_i$  for each document  $F_i$  in the dataset  $\mathcal{F}$ , the first step is to map the keyword set extracted from the document  $F_i$  to a data vector  $D_i$ , followed by encrypting every data vector. The time cost of mapping or encrypting depends directly on the dimensionality of data vector which is determined by the size of the dictionary, i.e., the number of indexed keywords. And the time cost of building the whole index is also related to the number of subindex which is equal to the number of documents in the dataset. Fig. 4(a) shows that, given the same dictionary where  $|\mathcal{W}| = 4000$ , the time cost of building the whole index is nearly linear with the size of dataset since the time cost of building each subindex is fixed. Fig. 4(b) shows that the number of keywords indexed in the dictionary determines the time cost of building a subindex. As presented in the section IV-A, the major computation to generate a subindex in MRSE\_I includes the splitting process and two multiplications of a  $(n+2) \times (n+2)$  matrix and a  $(n+2)$ -

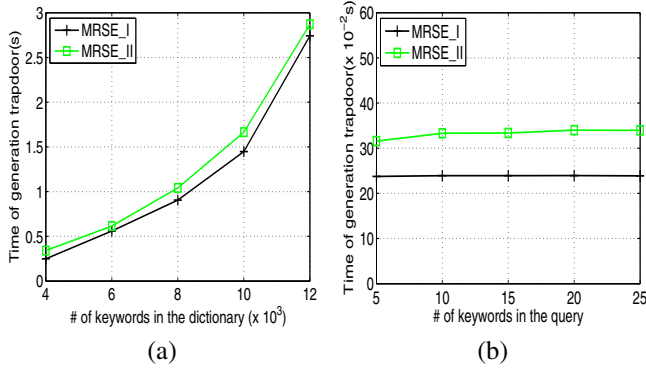


Fig. 5: Time cost of generating trapdoor. (a) For the same query keywords within different sizes of dictionary,  $t = 10$ . (b) For different numbers of query keywords within the same dictionary,  $n = 4000$ .

dimension vector where  $n = |\mathcal{W}|$ , both of which have direct relationship with the size of dictionary. The dimensionality of matrices in MRSE\_II is  $(n + U + 1) \times (n + U + 1)$  which is bigger than that in MRSE\_I so that the index construction time becomes larger as shown in both Fig. 4(a) and Fig. 4(b). Although the time of building index is not a negligible overhead for the data owner, this is a one-time operation before data outsourcing. Besides, Tab. III lists the storage overhead of each subindex in two MRSE schemes within different sizes of dictionary. The size of subindex is absolutely linear with the dimensionality of data vector which is determined by the number of keywords in the dictionary. The sizes of subindex are very close in the two MRSE schemes because of trivial differences in the dimensionality of data vector.

2) *Trapdoor Generation*: Fig. 5(a) shows that the time to generate a trapdoor is greatly affected by the number of keywords in the dictionary. Like index construction, every trapdoor generation incurs two multiplications of a matrix and a split query vector, where the dimensionality of matrix or query vector is different in two proposed schemes and becomes larger with the increasing size of dictionary. Fig. 5(b) demonstrates the trapdoor generation cost in the MRSE\_II scheme is about 20 percentages larger than that in the MRSE\_I scheme. Like the subindex generation, the difference of costs to generate trapdoors is majorly caused by the different dimensionality of vector and matrices in the two MRSE schemes. More importantly, it shows that the number of query keywords has little influence on the overhead of trapdoor generation, which is a significant advantage over related works on multi-keyword searchable encryption.

3) *Query*: Query execution in the cloud server consists of computing and ranking similarity scores for all documents in the dataset. Fig. 6 shows the query time is dominated by the number of documents in the dataset while the number of keywords in the query has very slight impact on it like the cost of trapdoor generation above. With respect to the communication cost in Query, the size of the trapdoor is

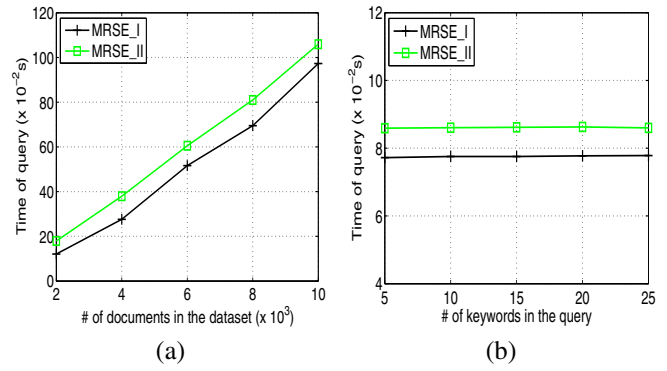


Fig. 6: Time cost of query. (a) For the same query keywords in different sizes of dataset,  $t = 10$ . (b) For different numbers of query keywords in the same dataset,  $m = 1000$ .

TABLE III: Size of subindex/trapdoor

Size of dictionary	4000	6000	8000	10000	12000
MRSE_I (KB)	31.3	46.9	62.5	78.1	93.8
MRSE_II (KB)	32.5	48.1	63.8	79.4	95.0

the same as that of the subindex listed in the Tab. III, which keeps constant given the same dictionary, no matter how many keywords are contained in a query. While the computation and communication cost in the query procedure is linear with the number of query keywords in other multiple-keyword search schemes [14], [16], our proposed schemes introduce nearly constant overhead while increasing the number of query keywords.

## VI. RELATED WORK

### A. Single Keyword Searchable Encryption

Traditional single keyword searchable encryption schemes [5]–[13], [22] usually build an encrypted searchable index such that its content is hidden to the server unless it is given appropriate trapdoors generated via secret key(s) [2]. It is first studied by Song et al. [5] in the symmetric key setting, and improvements and advanced security definitions are given in Goh [6], Chang et al. [7] and Curtmola et al. [8]. Our early work [22] solves secure ranked keyword search which utilizes keyword frequency to rank results instead of returning undifferentiated results. However, it only supports single keyword search. In the public key setting, Boneh et al. [9] present the first searchable encryption construction, where anyone with public key can write to the data stored on server but only authorized users with private key can search. Public key solutions are usually very computationally expensive however. Furthermore, the keyword privacy could not be protected in the public key setting since server could encrypt any keyword with public key and then use the received trapdoor to evaluate this ciphertext.

### B. Boolean Keyword Searchable Encryption

To enrich search functionalities, conjunctive keyword search [14]–[18] over encrypted data have been proposed.



These schemes incur large overhead caused by their fundamental primitives, such as computation cost by bilinear map, e.g. [16], or communication cost by secret sharing, e.g. [15]. As a more general search approach, predicate encryption schemes [19]–[21] are recently proposed to support both conjunctive and disjunctive search. Conjunctive keyword search returns “all-or-nothing”, which means it only returns those documents in which all the keywords specified by the search query appear; disjunctive keyword search returns undifferentiated results, which means it returns every document that contains a subset of the specific keywords, even only one keyword of interest. In short, none of existing Boolean keyword searchable encryption schemes support multiple keywords ranked search over encrypted cloud data while preserving privacy as we propose to explore in this paper. Note that, inner product queries in predicate encryption only predicates whether two vectors are orthogonal or not, i.e., the inner product value is concealed except when it equals zero. Without providing the capability to compare concealed inner products, predicate encryption is not qualified for performing ranked search. Furthermore, most of these schemes are built upon the expensive evaluation of pairing operations on elliptic curves. Such inefficiency disadvantage also limits their practical performance when deployed in the cloud. On a different front, the research on top- $k$  retrieval [26] in database community is also loosely connected to our problem.

## VII. CONCLUSION

In this paper, for the first time we define and solve the problem of multi-keyword ranked search over encrypted cloud data, and establish a variety of privacy requirements. Among various multi-keyword semantics, we choose the efficient similarity measure of “coordinate matching”, i.e., as many matches as possible, to effectively capture the relevance of outsourced documents to the query keywords, and use “inner product similarity” to quantitatively evaluate such similarity measure. For meeting the challenge of supporting multi-keyword semantic without privacy breaches, we propose a basic idea of MRSE using secure inner product computation. Then we give two significantly improved MRSE schemes to achieve various stringent privacy requirements in two different threat models. Thorough analysis investigating privacy and efficiency guarantees of proposed schemes is given, and experiments on the real-world dataset show our proposed schemes introduce low overhead on both computation and communication.

As our future work, we will explore supporting other multi-keyword semantics (e.g., weighted query) over encrypted data, integrity check of rank order in search result and privacy guarantees in the more stronger threat model.

## VIII. ACKNOWLEDGEMENTS

This work was supported in part by the US National Science Foundation under grants CNS-0716306, CNS-0831628, CNS-0746977, and CNS- 0831963.

## REFERENCES

- [1] L. M. Vaquero, L. Rodero-Merino, J. Caceres, and M. Lindner, “A break in the clouds: towards a cloud definition,” *ACM SIGCOMM Comput. Commun. Rev.*, vol. 39, no. 1, pp. 50–55, 2009.
- [2] S. Kamara and K. Lauter, “Cryptographic cloud storage,” in *RLCPS, January 2010, LNCS. Springer, Heidelberg*.
- [3] A. Singhal, “Modern information retrieval: A brief overview,” *IEEE Data Engineering Bulletin*, vol. 24, no. 4, pp. 35–43, 2001.
- [4] I. H. Witten, A. Moffat, and T. C. Bell, “Managing gigabytes: Compressing and indexing documents and images,” Morgan Kaufmann Publishing, San Francisco, May 1999.
- [5] D. Song, D. Wagner, and A. Perrig, “Practical techniques for searches on encrypted data,” in *Proc. of S&P*, 2000.
- [6] E.-J. Goh, “Secure indexes,” Cryptology ePrint Archive, 2003, <http://eprint.iacr.org/2003/216>.
- [7] Y.-C. Chang and M. Mitzenmacher, “Privacy preserving keyword searches on remote encrypted data,” in *Proc. of ACNS*, 2005.
- [8] R. Curtmola, J. A. Garay, S. Kamara, and R. Ostrovsky, “Searchable symmetric encryption: improved definitions and efficient constructions,” in *Proc. of ACM CCS*, 2006.
- [9] D. Boneh, G. D. Crescenzo, R. Ostrovsky, and G. Persiano, “Public key encryption with keyword search,” in *Proc. of EUROCRYPT*, 2004.
- [10] M. Bellare, A. Boldyreva, and A. O’Neill, “Deterministic and efficiently searchable encryption,” in *Proc. of CRYPTO*, 2007.
- [11] M. Abdalla, M. Bellare, D. Catalano, E. Kiltz, T. Kohno, T. Lange, J. Malone-Lee, G. Neven, P. Paillier, and H. Shi, “Searchable encryption revisited: Consistency properties, relation to anonymous ibe, and extensions,” *J. Cryptol.*, vol. 21, no. 3, pp. 350–391, 2008.
- [12] J. Li, Q. Wang, C. Wang, N. Cao, K. Ren, and W. Lou, “Fuzzy keyword search over encrypted data in cloud computing,” in *Proc. of IEEE INFOCOM’10 Mini-Conference*, San Diego, CA, USA, March 2010.
- [13] D. Boneh, E. Kushilevitz, R. Ostrovsky, and W. E. S. III, “Public key encryption that allows pir queries,” in *Proc. of CRYPTO*, 2007.
- [14] P. Golle, J. Staddon, and B. Waters, “Secure conjunctive keyword search over encrypted data,” in *Proc. of ACNS*, 2004, pp. 31–45.
- [15] L. Ballard, S. Kamara, and F. Monrose, “Achieving efficient conjunctive keyword searches over encrypted data,” in *Proc. of ICICS*, 2005.
- [16] D. Boneh and B. Waters, “Conjunctive, subset, and range queries on encrypted data,” in *Proc. of TCC*, 2007, pp. 535–554.
- [17] R. Brinkman, “Searching in encrypted data,” in *University of Twente, PhD thesis*, 2007.
- [18] Y. Hwang and P. Lee, “Public key encryption with conjunctive keyword search and its extension to a multi-user system,” in *Pairing*, 2007.
- [19] J. Katz, A. Sahai, and B. Waters, “Predicate encryption supporting disjunctions, polynomial equations, and inner products,” in *Proc. of EUROCRYPT*, 2008.
- [20] A. Lewko, T. Okamoto, A. Sahai, K. Takashima, and B. Waters, “Fully secure functional encryption: Attribute-based encryption and (hierarchical) inner product encryption,” in *Proc. of EUROCRYPT*, 2010.
- [21] E. Shen, E. Shi, and B. Waters, “Predicate privacy in encryption systems,” in *Proc. of TCC*, 2009.
- [22] C. Wang, N. Cao, J. Li, K. Ren, and W. Lou, “Secure ranked keyword search over encrypted cloud data,” in *Proc. of ICDCS’10*, 2010.
- [23] S. Yu, C. Wang, K. Ren, and W. Lou, “Achieving secure, scalable, and fine-grained data access control in cloud computing,” in *Proc. of INFOCOM*, 2010.
- [24] C. Wang, Q. Wang, K. Ren, and W. Lou, “Privacy-preserving public auditing for data storage security in cloud computing,” in *Proc. of INFOCOM*, 2010.
- [25] S. Zerr, E. Demidova, D. Olmedilla, W. Nejdl, M. Winslett, and S. Mitra, “Zerber: r-confidential indexing for distributed documents,” in *Proc. of EDBT*, 2008, pp. 287–298.
- [26] S. Zerr, D. Olmedilla, W. Nejdl, and W. Siberski, “Zerber+r: Top-k retrieval from a confidential index,” in *Proc. of EDBT*, 2009, pp. 439–449.
- [27] Y. Ishai, E. Kushilevitz, R. Ostrovsky, and A. Sahai, “Cryptography from anonymity,” in *Proceedings of the 47th Annual IEEE Symposium on Foundations of Computer Science*, 2006, pp. 239–248.
- [28] W. K. Wong, D. W. Cheung, B. Kao, and N. Mamoulis, “Secure knn computation on encrypted databases,” in *Proceedings of the 35th SIGMOD international conference on Management of data*, 2009, pp. 139–152.
- [29] W. W. Cohen, “Enron email dataset,” <http://www.cs.cmu.edu/~enron/>.